

# The Provincial Indices of Multiple Deprivation for South Africa 2001

### **Technical Report**

Michael Noble, Miriam Babita, Helen Barnes, Chris Dibben, Wiseman Magasela, Stefan Noble, Phakama Ntshongwana, Heston Phillips, Sharmla Rama, Benjamin Roberts, Gemma Wright and Sibongile Zungu





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#### Introduction

This technical report has been produced to provide further detail on the sensitivity testing carried out and the main methodological issues considered during the construction of the Provincial Indices of Deprivation for South Africa 2001 (PIMD 2001). This report should be read in conjunction with the PIMD 2001 report (Noble et al., 2005).

The PIMD 2001 has been produced by a group of researchers at the Centre for the Analysis of South African Social Policy (CASASP) in the Department of Social Policy and Social Work at the University of Oxford, the Human Sciences Research Council (HSRC) and Statistics South Africa (Stats SA). The project team comprised Michael Noble, Helen Barnes, Chris Dibben, Wiseman Magasela, Stefan Noble, Phakama Ntshongwana and Gemma Wright from CASASP at the University of Oxford; Benjamin Roberts and Sharmla Rama from the HSRC; and Miriam Babita, Heston Phillips and Sibongile Zungu from Stats SA.

Each PIMD is a relative measure of multiple deprivation for a particular province in South Africa and has been produced at ward level using the 2001 Census.

This report is divided into two sections. Section 1 covers sensitivity testing relating to the domains and indicators used in the PIMD, and Section 2 discusses methodological issues. The sensitivity testing in **Section 1** was carried out at municipality level on the 10% sample of the Census as there was only limited access to the 100% Census. The analysis in **Section 2** was carried out at ward level using the 100% Census.

In Section 3 maps showing the ward level PIMD 2001 for each province in South Africa are presented. These are more detailed than the maps presented in the full report as they show the major roads in each province (the deciles and boundaries are exactly the same as the maps in the full report however)<sup>1</sup>.

downloading.

<sup>&</sup>lt;sup>1</sup> If this report has been obtained from the internet, the maps are instead available as separate files for

#### **Section 1: Domains and Indicators**

## Income and Material Deprivation Domain: imputation of the income variable

One of the main difficulties in producing indicators of well-being (e.g. the low income indicator in the Income and Material Deprivation Domain) from the 2001 Census is the large proportion of missing values on a number of key variables such as age, education and income. In the 2001 Census, data on personal income were obtained by asking each person in the household "What is the income category that best describes the gross income of (this person) before tax?" The answer was recorded in income bands for each person. The use of the income data from the Census is problematic as there is a large proportion of missing income data (16% of individuals in the 10% sample) and a large proportion of incomes reported to be zero (50.1% of individuals aged 18 and over). It is difficult to determine a priori whether reported zero incomes are actual observed levels or whether it is due to the reluctance of people to reveal their true income. Non-response or invalid income values can bias well-being indicators if data are not missing completely at random.<sup>2</sup>

There are various ways of dealing with missing data. Davern et al. (2001) describe four main methods used:

- 1. Analyse complete cases only;
- 2. Only use cases with reported data on the problematic item;
- 3. Weight complete cases to make up for missing cases;
- 4. Impute missing data values.

Imputation is generally preferred when (a) there is a substantial proportion of non-response or missing data (more than 10%); (b) imputation can correct for potential distributional differences between respondents with missing data and those with reported data; and (c) it is possible to maintain relationships among associated variables. Given that the proportion of missing data is large in the 2001 Census, the preferred solution to the problem is to impute the missing values. There are various methods for imputing data and the best imputation method depends on the type of missing data.

Before releasing any Census products Statistics South Africa (Stats SA) adjusted for non-response using a logical imputation method and a single 'hot-deck' imputation. The former replaces missing data using information from other variables available in the dataset. Single hot-deck imputation involves matching, as closely as possible, individuals with missing data on some variables to individuals who have complete records, and using the information from the latter to replace the missing values in the former. This procedure is particularly suitable when data are missing at random

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<sup>&</sup>lt;sup>2</sup> Missing completely at random means that the probability of an item being missing is unrelated to any observed or unobserved characteristic for that unit.

(MAR)<sup>3</sup> and when the number of outliers is small. When these conditions are not met individuals with missing data may be inappropriately matched to individuals with complete records who are outliers or for whom the information recorded is incorrect.

Although the pattern of missing data fulfils the MAR assumption required by the hot-deck imputation method (and in general by other imputation methods), there is no way to assess a priori the reliability of the data imputed, that is whether there is a large proportion of outliers in the data that could potentially bias the imputed values. Furthermore, single hot-deck imputations do not provide a measure of the variance introduced with the imputation process.

The total variance introduced by imputing values can be estimated by repeating the imputation process a number of times, and the possible bias caused by the outliers in the data can be minimised. This technique is known as multiple imputation. To assess the reliability of the reported zero income, zero values can be set to missing and the values imputed, thereby checking whether the original value of zero was accurate. The imputation analysis on the income variable in the Census for the PIMD 2001 was performed on both original missing incomes and 'implausible' zero incomes. The implausible zero incomes were defined according to rules given by Ardington *et al.* (2005):

- 1. If household income was zero, income was set to missing for household members aged 15 and older and to zero for those younger than 15.
- 2. For those younger than 15 with recorded income greater than R6 400 per month, income was set to missing.
- 3. For those recorded as being employed but with zero income, income was set to missing.

In total, 27.1% of individuals in the 10% sample had either missing or implausible income data.<sup>4</sup>

This analysis used the sequential regression multiple imputation (SRMI) method developed by Raghunathan *et al.* (2001) to impute the missing values. The software used in the imputation was IVEware, which was developed exclusively to perform SRMI imputations.<sup>5</sup> There are three main reasons why SRMI is preferred to other multiple imputation methods. First, SRMI is a multiple imputation technique which allows estimation of the variance introduced in the imputations. Second, SRMI can handle very complex data structures (e.g. count, binary, continuous and categorical variables) that other imputation methods find problematic. Third, given that SRMI imputes values through a sequence of multiple regressions, covariates include all other variables observed and imputed from previous rounds. This sequence of

<sup>4</sup> Although a high proportion of individuals reported zero income, not all of these were defined as implausible and recoded as missing according to Ardington *et al*'s rules.

<sup>&</sup>lt;sup>3</sup> Missing at random means that the probability of an item being missing depends only on other items that have been observed for that unit and no additional information as to the probability of being missing would be obtained from the unobserved values of the missing items.

<sup>&</sup>lt;sup>5</sup> The imputation was run on the Unix computer at the Oxford Supercomputing Centre (OSC), University of Oxford. The team wish to acknowledge OSC for the use of their resources and in particular to thank Jon Lockley and his team at OSC for their help and support.

imputing missing values builds interdependence among imputed values and exploits the correlation structure among covariates (Raghunathan *et al.*, 2001).

For this analysis, the aim was not only to impute missing income, but also to impute the variables that could be used as explanatory variables of income such as age, gender, years of education, population group, province, etc. In this case the SRMI method divides the dataset into two matrices, one composed of all the variables that contain missing data, denoted by Y and another matrix composed of variables that have no missing data, denoted by X.

All variables included in the matrix Y are ordered from least to most missing values, i.e.  $Y_1$ ,  $Y_2$ ,  $Y_3$ ,  $Y_4$ ,  $Y_n$  and all Y variables are considered to be dependent variables to which missing values are imputed by maximizing the joint conditional density of matrix Y given matrix X. Each of the variables included in matrix Y can have a different type of distribution, such as dichotomous (e.g. gender), categorical (e.g. banded income) or continuous (e.g. age). These dependent variables are estimated using the type of regression model that most suits them. For instance, dichotomous variables are estimated using logit regression models, continuous variables are estimated using OLS regression models and so on.

In this method the imputation is performed in a series of steps and rounds. The first step is to estimate the missing values of  $Y_I$  given the variables in the X matrix. This step consists of up to 250 maximum likelihood iterations, which are needed for maximizing the joint conditional density of  $Y_I$  given matrix X. This is then followed by an estimate of  $Y_2$  given X and the newly derived  $\hat{Y}_I$  which contains both observed and imputed values (in other words  $\hat{Y}_I$  is included in the X matrix). The first round of imputations,  $\hat{Y}^{R=I}$ , is completed once each of the variables included in the Y matrix is estimated, as in the steps explained above. This first round of imputation contains no missing values and is equivalent to the single vector of hot deck imputations derived by Stats SA.

In the second round,  $Y_I$  is re-estimated including all first round  $\hat{Y}^{R=I}$  imputations on the right hand side. The first round missing value imputations for  $Y_I$  are replaced by a new set of imputations derived from this re-estimation. The new imputed values are conditional on the previously imputed values of the preceding imputation round. Figure 1.1 shows the variables that were imputed and the regression types that were used.

Each round of imputations produces individual values of matrix  $\hat{Y}$ , which contain no missing values and from which it is then possible to carry out further analysis such as measuring poverty or inequality. The imputed values for each variable may differ from round to round, and hence the estimated level of poverty, for example, may also differ from one round to another. The uncertainty about the actual level of poverty, say, is overcome by obtaining an estimate of poverty from every round, and then averaging over these estimates. The standard error of the resulting estimate of (average) poverty is obtained using the multiple imputation rule developed by Little and Rubin (2000). This rule applies to the derived measures only, like poverty and inequality, and not to the imputed values that were obtained.

Figure 1.1: Variables with missing data to be imputed

Y Matrix*	Regression Type	X Matrix
Age	OLS	Province
Gender	Logit	Location
Population group	Logit	
<b>Employment status</b>	Logit	
Occupation	Logit	
Education	OLS	
Income	Logit	
	-	

<sup>\*</sup> Variables ordered from least to most number of missing cases.

The imputation results produced in this work are very similar to those of Stats SA and of Ardington *et al.* (2005). Ardington *et al.* also employed the SRMI imputation method, but used different types of regression in the sequence of imputation and different software than in the analysis for the PIMD 2001.

The tables below compare the proportion of cases in each income band obtained by the PIMD 2001 analysis and Stats SA's hot deck imputation (the last column in the first table shows the proportion in each income band when no imputation or recoding of implausible zeros had taken place). The first table shows the distribution of income for all cases (i.e. imputed and not imputed cases), while the second table shows the distribution for the imputed cases only (i.e. the missing and implausible zero cases).

All three methods (Ardington *et al*'s results are not shown) assign roughly the same proportion of people overall to the first three income bands (84 to 85%). For the imputed cases only the proportion of people in the first three income bands ranges from 90 to 98%. In terms of the zero incomes, for each method between 65 and 69% of people overall either reported having no income or were placed in the zero income band by the imputation process. For the imputed cases only the proportion of people assigned to the zero income band is very similar for all three methods (79 to 81%).

The similarity between the results of Ardington *et al.* and this work is reassuring, but more surprising is the fact that the imputation results are also similar to those obtained using the single hot-deck imputation method. This is likely to reflect the fact that the number of outliers among the observations on the variables used for imputation was not large. Therefore, the large number of zero incomes reported are indeed reasonably accurate and do not represent outliers. Given the similarity in the results it was felt it would be acceptable to produce the Income and Material Deprivation Domain using Stats SA's hot deck imputations, rather than run the sequential regression multiple imputation on the full Census. **See page 17 of the full report.** 

Table 1.1: Observed and imputed cases

	SR	RMI	Hot deck imputation		I	
Income	PIMD on 10% Census with 10 imputations (imputation 10)		Census with 10 imputation (imputation 10)		10% Census	
band	%	Cum %	%	Cum %	%	Cum %
1	66.66	66.66	69.34	69.34	67.20	67.20
2	6.70	73.36	5.33	74.68	5.57	72.78
3	11.94	85.30	9.67	84.35	10.42	83.19
4	5.04	90.34	5.14	89.49	5.60	88.80
5	4.18	94.52	4.43	93.93	4.77	93.57
6	3.01	97.53	3.28	97.21	3.49	97.06
7	1.55	99.08	1.73	98.94	1.83	98.89
8	0.57	99.65	0.65	99.59	0.68	99.57
9	0.20	99.85	0.22	99.81	0.24	99.81
10	0.08	99.93	0.09	99.90	0.09	99.90
11	0.06	99.99	0.07	99.97	0.07	99.97
12	0.02	100.00	0.03	100.00	0.03	100.00

**Table 1.2: Imputed cases only** 

Income	with 10 i	10% Census mputations ation 10)	Stats SA on 10% Census with 1 imputation		
band	%	Cum %	%	Cum %	
1	79.00	79.00	80.95	80.95	
2	7.35	86.35	4.03	84.98	
3	11.61	97.96	5.62	90.61	
4	1.15	99.11	2.67	93.27	
5	0.57	99.68	2.59	95.86	
6	0.22	99.90	2.12	97.98	
7	0.05	99.95	1.21	99.19	
8	0.01	99.96	0.47	99.66	
9	0.00	99.96	0.15	99.81	
10	0.00	99.96	0.07	99.88	
11	0.03	99.99	0.09	99.98	
12	0.00	100.00	0.02	100.00	

#### Income and Material Deprivation Domain: equivalence scales

The living standard of an individual depends not only on their own income, but also on the income of others in the household. In the South African context this is especially true and it is well documented that household resources are often pooled. Since households vary by size and demographic composition, simply using total household income as an indicator would produce misleading results. Consequently, it has become customary to use some form of adjustment to take into account variations in household size and/or composition (usually age i.e. whether people are adults or children). It is argued that the needs of a household increase with each additional member, but not in a proportional way due to economies of scale. In order to enjoy a comparable standard of living, a household with several adults will need a higher income than a single person living alone. However, the needs of a household with three members will not be three times higher than those of a single person.

The simplest type of adjustment entails dividing total household income by household size to produce a per capita measure. However, while this takes into account household size, it does not adjust for structure, thus assigning equal values for adults and children alike under the assumption that there is no sharing of resources within the household.

More complex equivalence scales assign values to each household in proportion to its needs, taking into account both size of the household and the age of its members (number of adults and children). Equivalence scales conventionally take a couple as the reference point and assign an equivalence value of one. The process then increases relatively the income of single person households and reduces relatively the incomes of households with more than one person.

Since there are a wide variety of possible equivalence scales, the selection of a particular one is premised upon a set of assumptions about economies of scale and value judgements about the priority of the differential needs of individuals (children versus adults). As such judgements may affect results, sensitivity testing was conducted to determine whether relative ranking is affected by the use of different equivalence scale parameters. This work had to be undertaken at the municipality level on the 10% sample of the Census as there was limited access to the 100% Census.

Five different equivalence scales were tested to see what, if any, impact they had on the overall Income and Material Deprivation Domain. These are explained in more detail below, and their impact analysed.

### (i) Household equivalent income of less than 40% of mean equivalent household income (equivalised using the modified OECD equivalence scale)

To calculate this income measure, logarithmic mean values<sup>6</sup> were assigned to the income bands. Next an annual household income was calculated by summing the individual income of each person in the household. The modified OECD scale<sup>7</sup> was then used to create an equivalence factor:

Equivalence factor = 1 + (number of people over 14 years \* 0.5) + (number of people under 14 years \* 0.3)

This gives greatest weight to the first adult and less to subsequent adults and children over 14 years. The lowest weight goes to children under 14 years. The annual household income was divided by the equivalence factor to give a household equivalent income. Finally, any person with a household equivalent income of less than 40% of mean equivalent household income was defined as income deprived.

### (ii) Household equivalent income of less than 40% of mean equivalent household income (equivalised using the old OECD equivalence scale)

This measure was calculated in exactly the same way as for (i). The old OECD equivalence factor is:

Equivalence factor =  $1 + (number\ of\ adults\ *0.7) + (number\ of\ children\ *0.5)$ 

This gives greatest weight to the first adult and less to subsequent adults. The lowest weight goes to children.

## (iii) Household equivalent income of less than 40% of mean equivalent household income (equivalised using the square root scale)

This equivalence scale is different to the above two as it does not take into account the size and composition of the household in the same way. The scale divides household income by the square root of household size rather than assigning specific weights to adults and children:

*Equivalence factor = annual household income / square root of household size* 

This implies that, for example, a household of four people has needs twice as large as a single person household.

#### (iv) Per capita income of less than R 4 800 pa<sup>8</sup>

Annual household income was calculated in the same way as for the above three measures. Per capita income was calculated by dividing the annual household income

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<sup>&</sup>lt;sup>6</sup> See Census 2001 Metadata (information on households and housing) released by Stats SA for more information.

<sup>&</sup>lt;sup>7</sup> First proposed by Haagenars *et al.* (1994).

<sup>&</sup>lt;sup>8</sup> Both (iv) and (v) are used by Ardington *et al.* (2005) in their sensitivity testing of estimates of changes in poverty and inequality to imputation of the income variable in the Census.

by the number of people in the household. Any person with a per capita income of less than R 4 800 was defined as having low income.

*Equivalence factor = annual household income / number of people in household* 

#### (v) Per capita income of less than R 1 488 pa

This measure was calculated in exactly the same way as for (iv), but any person with a per capita income of less than R 1 488 was defined as having low income.

*Equivalence factor = annual household income / number of people in household* 

The tables below show the proportion captured by the low income indicator alone using the different equivalence scales<sup>9</sup> and the correlations between the five versions of the Income and Material Deprivation Domain. The income indicator for the first four versions captures approximately the same proportion of the population (between 67 and 73%). The per capita income of less than R 1488 pa is a more extreme measure and only captures 41% of the population. The Income and Material Deprivation Domains produced using the five different equivalence scales correlate very highly at municipality level across the country. The lowest correlations are the per capita measures (iv) and (v) with the other three measures, but even these are above 0.9. As mentioned above, the per capita equivalence scales do not adjust for household structure and so are a more crude measure than equivalence scales that take into account household size and structure. They were included in the sensitivity testing as an additional comparison only and not because it was felt that a per capita scale should possibly be used in the final PIMD 2001. The use of different equivalence scales appears to have little impact on the overall Income and Material Deprivation Domain and therefore little impact on the PIMD 2001.

Table 1.3: Proportion of the population captured when using different equivalence scales

Version	Proportion of population captured
(i) modified OECD	71.93
(ii) old OECD	72.53
(iii) square root scale	68.50
(iv) per capita income < R 4800 pa	67.93
(v) per capita income < R 1488 pa	41.11

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<sup>&</sup>lt;sup>9</sup> Figures are from the 10% sample of the Census (people in institutions excluded) and are **not** weighted to give a national figure.

Table 1.4: Income and Material Deprivation Domain correlations (Spearman's rho) for each equivalence scale

	(i)	(ii)	(iii)	(iv)	(v)
(i)	1.000	0.999	0.995	0.997	0.949
(ii)	0.999	1.000	0.994	0.996	0.946
(iii)	0.995	0.994	1.000	0.996	0.961
(iv)	0.997	0.996	0.996	1.000	0.962
(v)	0.949	0.946	0.961	0.962	1.000

All correlations are significant at the 0.01 level

The modified OECD equivalence scale was used in the Income Domain in the PIMD 2001 because it is widely used internationally. **See pages 17-18 of the full report.** 

#### **Income and Material Deprivation Domain: income thresholds**

Income deprivation is often measured as the proportion of households living below a particular low income threshold, most often the proportion below various fractions (usually ranging from 40 to 60 %) of median or mean income. Before selecting a particular threshold, sensitivity testing was conducted to determine whether relative ranking was changed by employing different income thresholds (20%, 30% and 40% of equivalised household mean income). The modified OECD equivalence scale (see previous section) was applied in all cases. This work had to be undertaken at the municipality level on the 10% sample of the Census as there was limited access to the 100% Census.

The following table shows the proportion of the population captured by the low income indicator alone using different income thresholds. <sup>10</sup> The correlations between the three versions are high (Table 1.6), which suggests that the use of different income thresholds appears to have little impact on the overall Income and Material Deprivation Domain and therefore little impact on the PIMD 2001.

Table 1.5: Proportion of the population captured when using different income thresholds

Version	Proportion of population captured
20% equivalised household mean income	55.97
30% equivalised household mean income	66.30
40% equivalised household mean income	71.93

Table 1.6: Income and Material Deprivation Domain correlations (Spearman's rho) for each income threshold

	20%	30%	40%
20%	1.000	0.989	0.977
30%	0.989	1.000	0.994
40%	0.977	0.994	1.000

All correlations are significant at the 0.01 level

The 40% threshold was used for the low income indicator in the PIMD 2001 because it is one of the most commonly used thresholds internationally. The other internationally recognised thresholds (50% and 60%) would have captured too great a proportion of the population for many wards and therefore would have been insufficiently discriminating. See page 17 of the full report.

 $<sup>^{10}</sup>$  Figures are from the 10% sample of the Census (people in institutions excluded) and are **not** weighted to give a national figure.

#### **Employment Deprivation Domain: definition of unemployment**

Sensitivity testing was conducted to determine whether relative ranking was changed by using the expanded definition of unemployment rather than the official definition. This work had to be undertaken at the municipality level on the 10% sample of the Census as there was limited access to the 100% Census.

The official definition of employment defines the unemployed as people within the economically active population who (a) did not work in the seven days prior to Census night, (b) wanted to work and were available to start work within a week of Census night, and (c) had taken active steps to look for work or start some form of self-employment in the four weeks prior to Census night (e.g. registration at an employment exchange, applications to employers, checking at work sites or farms, placing or answering newspaper advertisements, seeking assistance of friends, etc).

The expanded definition of unemployment defines the unemployed as people who fulfil (a) and (b) above but did not take active steps to seek work. This broad definition captures discouraged work seekers, and those without the resources to take active steps to seek work.

Two versions of the Employment Deprivation Domain were created; one using the official definition, and one using the expanded definition. The two versions correlate very highly (0.990 Spearman's rho, p=0.01). The use of the different unemployment definitions appears to have little impact on the overall Employment Deprivation Domain and therefore little impact on the PIMD 2001.

The proportion of the relevant population (people aged 15-65 inclusive) captured by the official definition of unemployment is 15.27% (this is the figure for the unemployed only and not the additional people included in the numerator who are not working because they are ill or disabled). For the expanded definition of unemployment the proportion is 18.71%. Therefore, even using the expanded definition, only approximately 3.5% more of the relevant population are captured.

The official definition of unemployment was used in the PIMD 2001 as it is more commonly used by the main potential users of Indices (the three spheres of Government) and the difference in *relative* terms between the official and the expanded definitions was negligible. **See page 19 of the full report.** 

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<sup>&</sup>lt;sup>11</sup> Figures are from the 10% sample of the Census (people in institutions excluded) and are **not** weighted to give a national figure.

#### **Health Deprivation Domain: shrinkage estimation**

The technique of shrinkage estimation was applied to the Health Deprivation Domain only. In some areas, particularly where populations at risk are small, data may be 'unreliable', that is more likely to be affected by measurement error or sampling error, with particular wards getting unrepresentatively low or high scores on certain indicators. The extent of a score's 'unreliability' can be measured by calculating its standard error.

This problem emerged in the construction of other indices in the past and this prompted the use of the signed chi squared statistic (see for example Robson, 1994). However, this technique has been much criticised for its use in this context because it conflates population *size* with *levels* of deprivation (see for example Connolly and Chisholm, 1999). Given the problems with the signed chi squared approach, another technique - 'shrinkage estimation' (i.e. empirical Bayesian estimation) - has been used subsequently to deal with the problem.<sup>12</sup>

Shrinkage involves moving unreliable ward scores (i.e. those with a high standard error) towards another more robust score. This may be towards more deprivation or less deprivation. There are many possible candidates for the more robust score to which an unreliable score could move. The municipality mean has been selected for this purpose but others could, in theory, include the South African mean, the province mean or the means of areas with similar characteristics.

Arguably, the movement of unreliable scores towards the mean score for South Africa would be inappropriate because of the large variation across the country and because it would be preferable to take into account local circumstances. 'Borrowing strength' from adjacent wards, though superficially attractive, could be problematic especially near the edges of towns. Though shrinking to the mean of wards with similar characteristics is attractive there are no recognised ward classification systems currently available.

It was concluded that shrinkage to the municipality mean was the best and most reliable procedure. This is in essence the same as shrinking to the population weighted ward mean for a municipality.

The actual mechanism of the procedure is to estimate deprivation in a particular ward using a weighted combination of (a) data from that ward and (b) data from the municipality. The weight attempts to increase the efficiency of the estimation, while not increasing its bias. If the ward has a high standard error and a municipality appears to be an unbiased estimation of the ward score then the ward score moves towards the municipality score.

<sup>&</sup>lt;sup>12</sup> For England see Noble, Smith *et al*, 2000a p16; Noble, Wright *et al*, 2004 p16; for Wales see Noble, Smith, Wright *et al*, 2000 p8; for Northern Ireland see Noble, Smith, Wright *et al*, 2001 p11; Noble, Barnes *et al*, 2005a p7; and for Scotland see Noble, Wright *et al*, 2003b p15.

Although most scores move a small amount, only unreliable scores, that is those with a large standard error, move significantly. The amount of movement depends on both the size of the standard error and the amount of heterogeneity amongst the wards in a municipality.

The 'shrunken' estimate of a ward-level proportion (or ratio) is a weighted average of the two 'raw' proportions for the ward and for the corresponding municipality. <sup>13</sup> The weights used are determined by the relative magnitudes of within-ward and betweenward variability.

The 'shrunken' ward-level estimate is the weighted average

$$z_{j}^{*} = w_{j}z_{j} + (1 - w_{j})z$$
 [1]

where  $z_j$  is the ward level proportion, z is the municipality level proportion,  $w_j$  is the weight given to the 'raw' ward-j data and  $(1-w_j)$  the weight given to the overall proportion for the municipality. The formula used to determine  $w_j$  is

$$w_j = \frac{1/s_j^2}{1/s_j^2 + 1/t^2}$$
 [2]

where  $s_j$  is the standard error of the ward level proportion, and  $t^2$  is the inter-ward variance for the k wards in the municipality, calculated as

$$t^2 = \frac{1}{k-1} \sum_{j=1}^{k} (z_j - z)^2$$
 [3]

The impact of shrinkage was tested on early versions of all domains, but it was found that there was very little movement in the scores, and so for transparency of method, the 'unshrunk' scores were used for all indicators, other than the Years of Potential Life Lost indicator in the Health Deprivation Domain where the 'shrunk' score was used.

The following scatterplots compare the shrunk (Y axis) and unshrunk (X axis) versions of each domain. For all domains except the Health Deprivation Domain, the line on the graph is fairly straight and there are few outliers. The unshrunk and shrunk scores for each of these four domains correlate 0.99 (Spearman's rho, p=0.01).

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<sup>&</sup>lt;sup>13</sup> Where appropriate the weighted average is calculated on the logit scale, for technical reasons, principally because the logit of a proportion is more nearly normally distributed than the proportion itself.

Chart 1.1: Shrunk scores against unshrunk scores for Income and Material Deprivation Domain

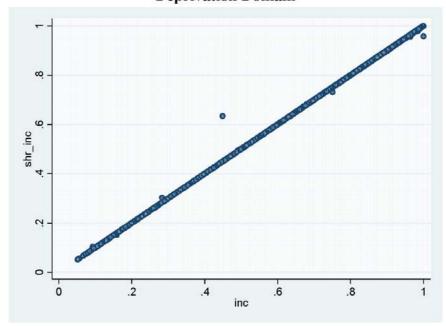


Chart 1.2: Shrunk scores against unshrunk scores for Employment Deprivation

Domain

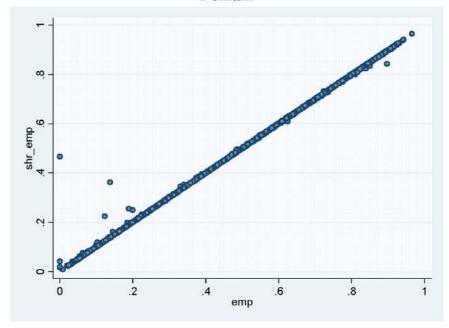


Chart 1.3: Shrunk scores against unshrunk scores for Education Deprivation

Domain

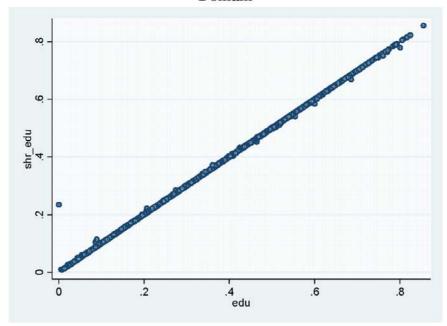
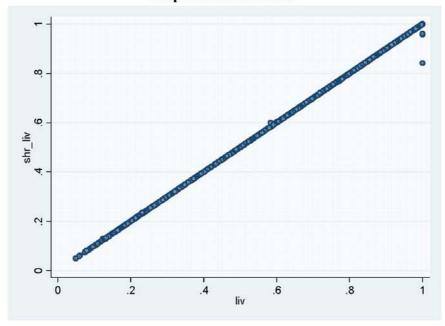


Chart 1.4: Shrunk scores against unshrunk scores for Living Environment Deprivation Domain



For the Health Deprivation Domain, there are a number of outliers which distort the picture to a certain extent (first scatterplot below), but even when these are removed, it is clear that the shrinkage estimation technique has done some work to move the unreliable scores (second scatterplot<sup>14</sup>). The unshrunk and shrunk scores (before

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<sup>&</sup>lt;sup>14</sup> Two outliers - a ward in Pilansberg National Park municipality and a ward in Giants Castle Game Reserve municipality - were removed. These are both DMAs and so will have been excluded from the

outliers removed) correlate 0.95 (Spearman's rho, p=0.01), with the Eastern Cape having the highest correlation (0.97) and the Western Cape the lowest (0.85).

Chart 1.5: Shrunk scores against unshrunk scores for Health Deprivation Domain

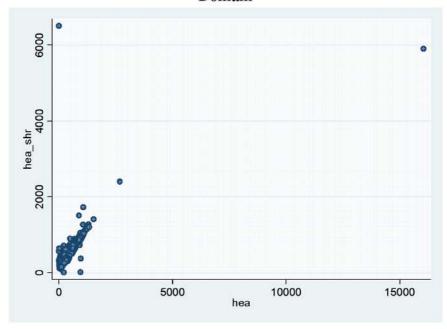
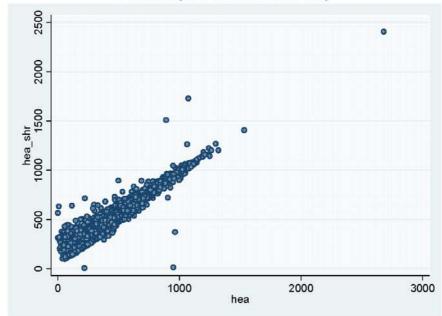


Chart 1.6: Shrunk scores against unshrunk scores for Health Deprivation Domain (two outliers removed)



See pages 21 and 27-28 of the full report.

PIMD 2001 in any case, along with other DMAs which are also outliers in the Health Deprivation Domain.

#### Living Environment Deprivation Domain: choice of indicators

The Census 2001 contains information on a variety of aspects relating to the living environment. From this information a number of potential indicators for the Living Environment Deprivation Domain were developed. However, the aim for each domain was to include a parsimonious (i.e. economical in number) collection of indicators that comprehensively captured the deprivation for each domain, but within the constraints of the data available from the Census. Therefore, decisions had to be made on which indicators to keep in the final PIMD 2001.

The following table shows the proportion of the population captured by each indicator used in the final PIMD, and also the proportion captured by other indicators considered (in italics). The proportion captured ranges from 10% to almost 60%.

Table 1.7: Proportion of the population captured by Living Environment Deprivation Domain indicators

Indicator	Proportion of population captured
No pit latrine with ventilation or flush toilet	46.12
No piped water inside dwelling or yard or within 200m	31.59
No electricity for lighting	29.99
Live in a shack	12.95
No access to a telephone	10.02
Two or more people per room	31.40
No rubbish removal by the local authority	47.72
One or more people per room	59.42
Three or more people per room	13.47
No flush toilet	52.52

While it is useful to know the proportion captured by each indicator in isolation, it is perhaps more helpful to know the proportion extra each indicator contributes to the overall proportion of deprived people within an area. This of course depends on the order in which the indicators are added. The table below shows the proportion extra of the population captured by each successive indicator, starting with the indicator measuring the lack of adequate toilet facility. Indicators are added (arguably) in order of importance.

<sup>&</sup>lt;sup>15</sup> Figures are from 10% sample of the Census (people in institutions excluded) and are **not** weighted to give a national figure.

Table 1.8: Proportion extra captured by adding more indicators

Indicator	Proportion extra of population captured	
No pit latrine with ventilation or flush toilet	46.12	
No piped water inside dwelling or yard or within 200m		5.03
No electricity for lighting		3.82
Live in a shack		3.06
No access to a telephone		0.68
Two or more people per room		8.07
No rubbish removal by the local authority		2.92

The rubbish removal indicator was dropped as there was concern about bias against urban areas and in any event it did not capture many additional people. See pages 23-24 of the full report.

### **Section 2: Methodology**

#### **Exponential transformation**

Once the domains had been constructed, it was necessary to combine them into an overall index for each province. In order to do this the domain indices were standardised by ranking. They were then transformed to an exponential distribution.

The exponential distribution was selected for the following reasons. First, it transforms each domain so that they each have a common distribution, the same range and identical maximum/minimum value, so that when the domains are combined into a single index of multiple deprivation the (equal) weighting is explicit; that is there is no implicit weighting as a result of the underlying distributions of the data. Second, it is not affected by the size of the ward's population. Third, it effectively spreads out the part of the distribution in which there is most interest; that is the most deprived wards in each domain.

Each transformed domain has a range of 0 to 100, with a score of 100 for the most deprived ward. The research team judged that the exponential transformation that stretched out or emphasised the most deprived 25% of wards would be most appropriate. When transformed scores from different domains are combined by averaging them, the skewness of the distribution reduces the extent to which deprivation on one domain can be cancelled by lack of deprivation on another. For example, if the transformed scores on two domains are averaged with equal weights, a (hypothetical) ward that scored 100 on one domain and 0 on the other would have a combined score of 50 and would thus be ranked at the 75th percentile. (Averaging the untransformed ranks, or after transformation to a normal distribution, would result in such a ward being ranked instead at the 50th percentile: the high deprivation in one domain would have been fully cancelled by the low deprivation in the other). Thus the extent to which deprivation in some domains can be cancelled by lack of deprivation in others is, by design, reduced.

The transformation used is as follows. For any ward, denote its rank on the domain, scaled to the range [0,1], by R (with R=1/N for the least deprived, and R=N/N, i.e. R=1, for the most deprived, where N=the number of wards in the province).

The transformed domain  $X = -\theta * \log\{1 - R*[1 - \exp(-100/\theta)]\}$ 

where log denotes natural logarithm and exp the exponential or antilog transformation and  $\theta$  is a constant which determines the slope of the exponential. For the PIMD (where the most deprived 25% of wards are emphasised)  $\theta$ =45.5.

The chosen exponential distribution is one of an infinite number of possible distributions. Two other exponentials were explored: stretching out the most deprived 10% of wards (used in UK Indices) and stretching out the most deprived 30% of wards. The three exponentials are compared below for two example provinces, the Western Cape and KwaZulu-Natal.

### **Western Cape**

Chart 2.1: PIMD (25%) with version accentuating 10% most deprived (pimd10)

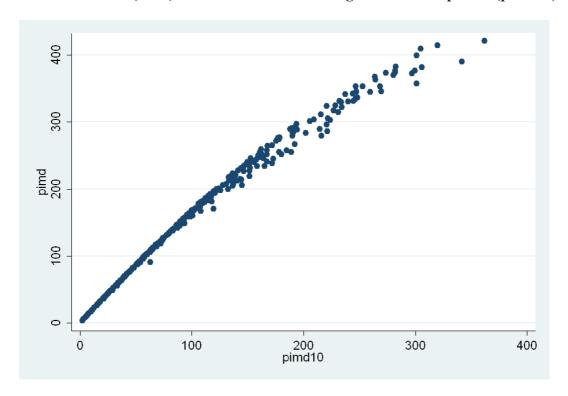
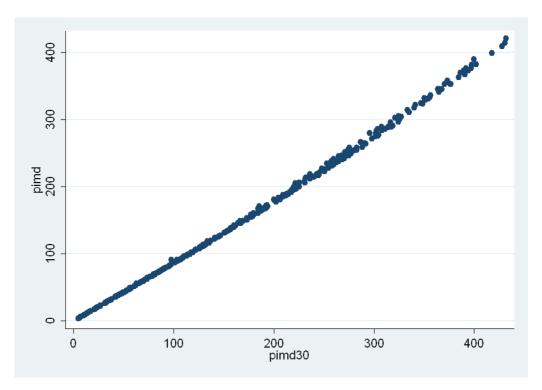


Chart 2.2: PIMD (25%) with version accentuating 30% most deprived (pimd30)



#### KwaZulu-Natal

Chart 2.3: PIMD (25%) with version accentuating 10% most deprived (pimd10)

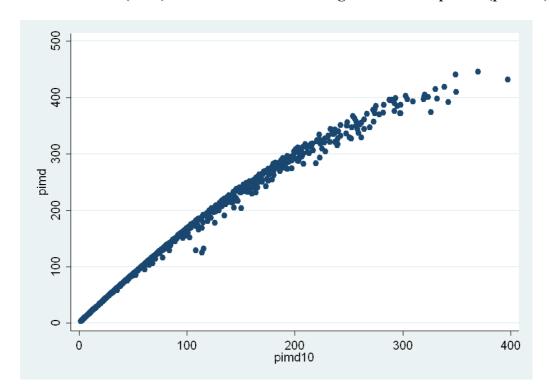
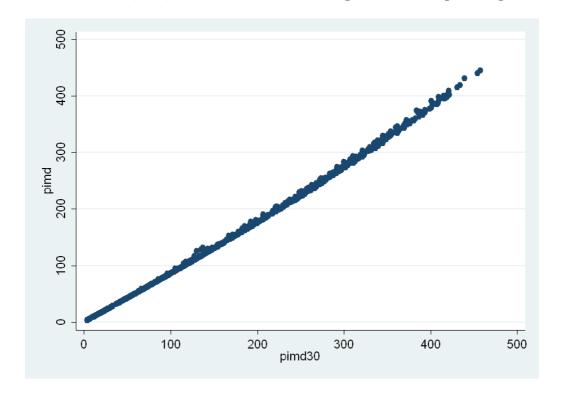


Chart 2.4: PIMD (25%) with version accentuating 30% most deprived (pimd30)



See pages 29-30 of the full report.

#### Correlations between domain scores and PIMD

The tables below show the correlations between the five domains and the PIMD for each province. In each province, all domains correlate fairly highly with the overall PIMD for that province. In all cases, the Income Deprivation Domain has the highest correlation with the PIMD (0.914 to 0.974) and also correlates highly with the Living Environment Deprivation Domain. In nearly all provinces the Employment Deprivation, Education Deprivation and Living Environment Deprivation Domains all have a correlation of over 0.7 with their respective PIMD, but the intra-domain correlations are not always as high. In most provinces the Health Deprivation Domain has the lowest correlation with its PIMD and all other domains.

#### Domain correlations (Spearman's rho) for each PIMD

<b>Table 2.1:</b>	Income	Employment	Health	Education	Living	PIMD
Western	Deprivation	Deprivation	Deprivation	Deprivation	Environment	
Cape					Deprivation	
Income	1.000	0.596	0.678	0.788	0.889	0.973
Deprivation						
Employment	0.596	1.000	0.403	0.171	0.580	0.637
Deprivation						
Health	0.678	0.403	1.000	0.474	0.573	0.771
Deprivation						
Education	0.788	0.171	0.474	1.000	0.736	0.767
Deprivation						
Living	0.889	0.580	0.573	0.736	1.000	0.915
Environment						
Deprivation						
PIMD	0.973	0.637	0.771	0.767	0.915	1.000

<b>Table 2.2:</b>	Income	Employment	Health	Education	Living	PIMD
Eastern	Deprivation	Deprivation	Deprivation	Deprivation	Environment	
Cape					Deprivation	
Income	1.000	0.847	0.667	0.859	0.897	0.960
Deprivation						
Employment	0.847	1.000	0.560	0.649	0.768	0.855
Deprivation						
Health	0.667	0.560	1.000	0.626	0.679	0.790
Deprivation						
Education	0.859	0.649	0.626	1.000	0.795	0.888
Deprivation						
Living	0.897	0.768	0.679	0.795	1.000	0.929
Environment						
Deprivation						
PIMD	0.960	0.855	0.790	0.888	0.929	1.000

<b>Table 2.3:</b>	Income	Employment	Health	Education	Living	PIMD
Northern	Deprivation	Deprivation	Deprivation	Deprivation	Environment	
Cape					Deprivation	
Income	1.000	0.568	0.523	0.732	0.672	0.934
Deprivation						
Employment	0.568	1.000	0.462	0.123*	0.128*	0.587
Deprivation						
Health	0.523	0.462	1.000	0.428	0.266	0.676
Deprivation						
Education	0.732	0.123*	0.428	1.000	0.746	0.781
Deprivation						
Living	0.672	0.128*	0.266	0.746	1.000	0.715
Environment						
Deprivation						
PIMD	0.934	0.587	0.676	0.781	0.715	1.000

<b>Table 2.4:</b>	Income	Employment	Health	Education	Living	PIMD
Free State	Deprivation	Deprivation	Deprivation	Deprivation	Environment Deprivation	
Income	1.000	0.599	0.537	0.668	0.838	0.937
Deprivation						
Employment	0.599	1.000	0.575	0.062*	0.412	0.614
Deprivation						
Health	0.537	0.575	1.000	0.305	0.422	0.697
Deprivation						
Education	0.668	0.062*	0.305	1.000	0.698	0.700
Deprivation						
Living	0.838	0.412	0.422	0.698	1.000	0.869
Environment						
Deprivation						
PIMD	0.937	0.614	0.697	0.700	0.869	1.000

<b>Table 2.5:</b>	Income	Employment	Health	Education	Living	PIMD
KwaZulu-	Deprivation	Deprivation	Deprivation	Deprivation	Environment	
Natal					Deprivation	
Income	1.000	0.855	0.545	0.874	0.913	0.962
Deprivation						
Employment	0.855	1.000	0.495	0.682	0.787	0.870
Deprivation						
Health	0.545	0.495	1.000	0.463	0.478	0.674
Deprivation						
Education	0.874	0.682	0.463	1.000	0.854	0.890
Deprivation						
Living	0.913	0.787	0.478	0.854	1.000	0.920
Environment						
Deprivation						
PIMD	0.962	0.870	0.674	0.890	0.920	1.000

<b>Table 2.6:</b>	Income	Employment	Health	Education	Living	PIMD
North West	Deprivation	Deprivation	Deprivation	Deprivation	Environment	
Province					Deprivation	
Income	1.000	0.704	0.602	0.825	0.716	0.958
Deprivation						
Employment	0.704	1.000	0.492	0.371	0.564	0.733
Deprivation						
Health	0.602	0.492	1.000	0.535	0.283	0.715
Deprivation						
Education	0.825	0.371	0.535	1.000	0.544	0.821
Deprivation						
Living	0.716	0.564	0.283	0.544	1.000	0.751
Environment						
Deprivation						
PIMD	0.958	0.733	0.715	0.821	0.751	1.000

<b>Table 2.7:</b>	Income	Employment	Health	Education	Living	PIMD
Gauteng	Deprivation	Deprivation	Deprivation	Deprivation	Environment Deprivation	
Income Deprivation	1.000	0.854	0.688	0.871	0.849	0.974
Employment Deprivation	0.854	1.000	0.719	0.632	0.626	0.849
Health Deprivation	0.688	0.719	1.000	0.614	0.464	0.787
Education Deprivation	0.871	0.632	0.614	1.000	0.846	0.901
Living Environment Deprivation	0.849	0.626	0.464	0.846	1.000	0.842
PIMD	0.974	0.849	0.787	0.901	0.842	1.000

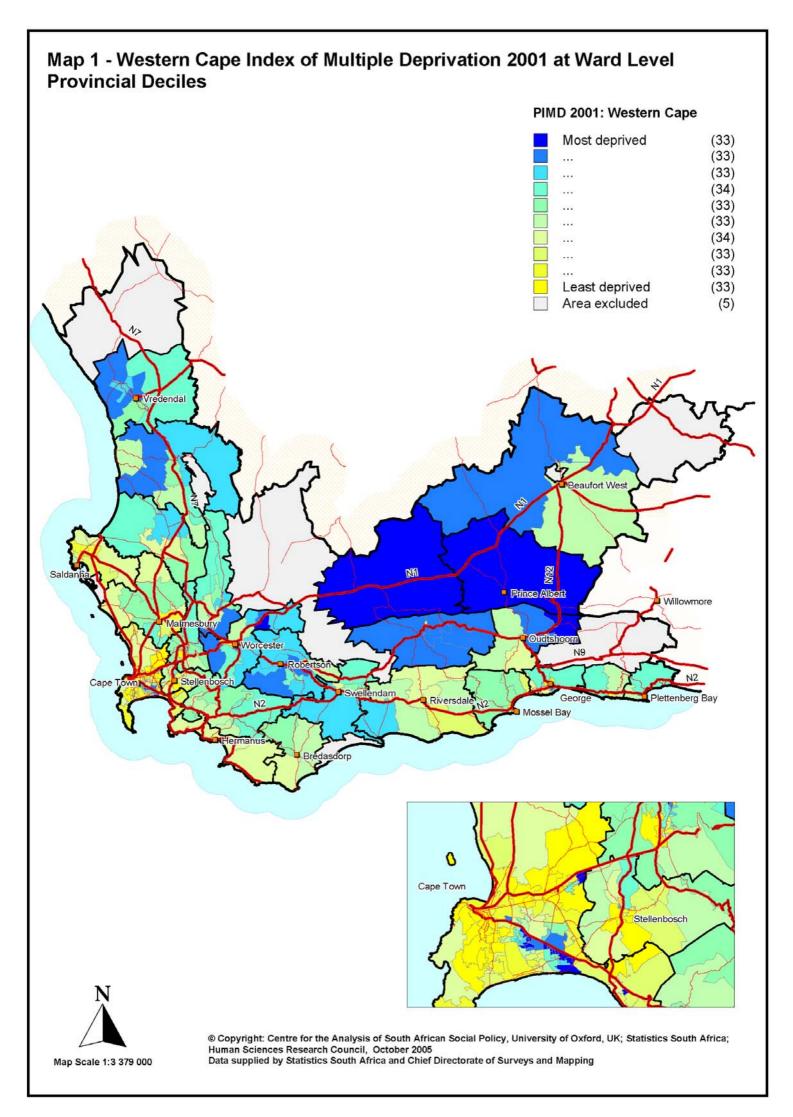
<b>Table 2.8:</b>	Income	Employment	Health	Education	Living	PIMD
Mpumalanga	Deprivation	Deprivation	Deprivation	Deprivation	Environment	
1 8					Deprivation	
Income	1.000	0.691	0.504	0.821	0.807	0.941
Deprivation						
Employment	0.691	1.000	0.379	0.434	0.592	0.741
Deprivation						
Health	0.504	0.379	1.000	0.494	0.334	0.638
Deprivation						
Education	0.821	0.434	0.494	1.000	0.682	0.836
Deprivation						
Living	0.807	0.592	0.334	0.682	1.000	0.835
Environment						
Deprivation						
PIMD	0.941	0.741	0.638	0.836	0.835	1.000

Table 2.9: Limpopo	Income Deprivation	Employment Deprivation	Health Deprivation	Education Deprivation	Living Environment Deprivation	PIMD
Income	1.000	0.727	0.292	0.661	0.734	0.915
Deprivation						
Employment	0.727	1.000	0.043*	0.443	0.636	0.734
Deprivation						
Health	0.292	0.043*	1.000	0.240	0.156	0.456
Deprivation						
Education	0.661	0.443	0.240	1.000	0.455	0.748
Deprivation						
Living	0.734	0.636	0.156	0.455	1.000	0.783
Environment						
Deprivation						
PIMD	0.915	0.734	0.456	0.748	0.783	1.000

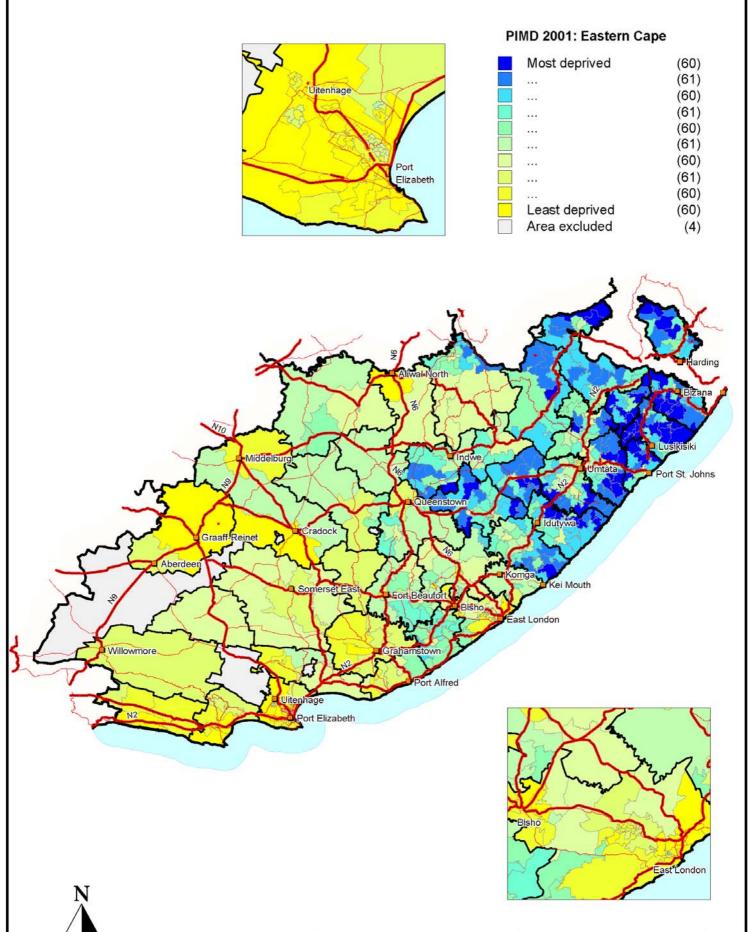
All correlations are significant at the 0.01 level (2-tailed) except where indicated by \*

See page 52 of the full report.

### **Section 3: Maps**



Map 2 - Eastern Cape Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles

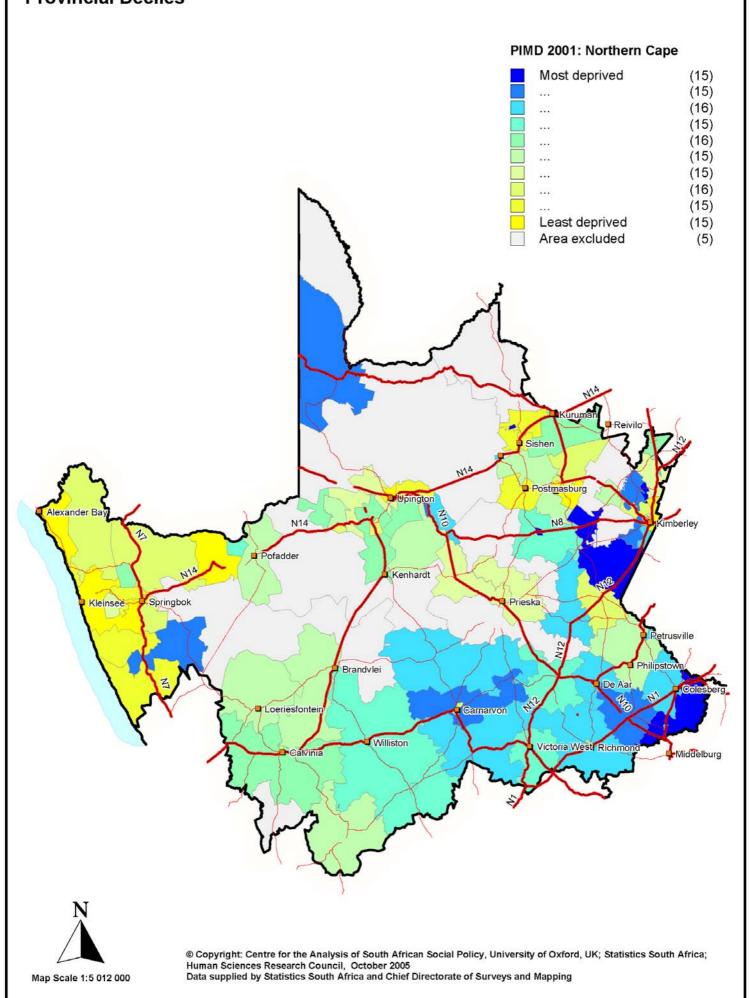


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Data supplied by Statistics South Africa and Chief Directorate of Surveys and Mapping

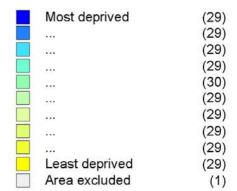
Map Scale 1:3 966 000

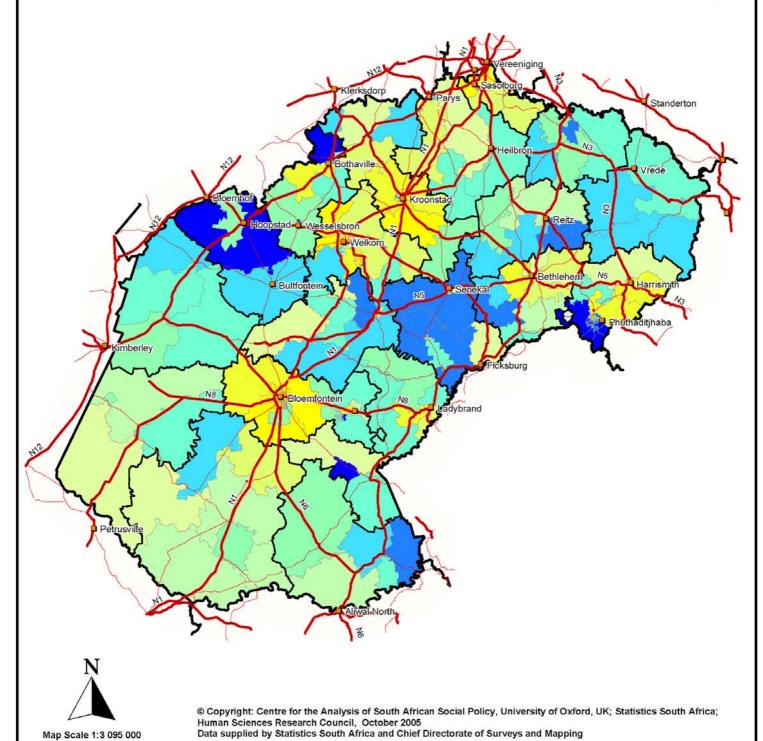
Map 3 - Northern Cape Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles



Map 4 - Free State Index of Multiple Deprivation 2001 at Ward Level **Provincial Deciles** 

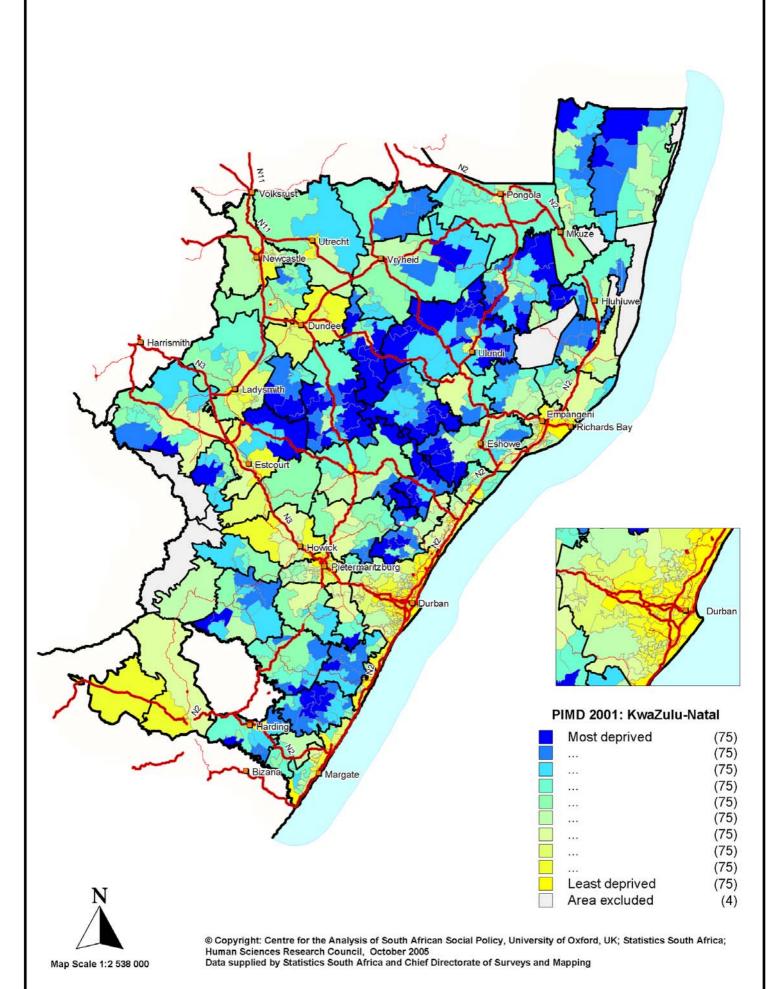
#### PIMD 2001: Free State





Map Scale 1:3 095 000

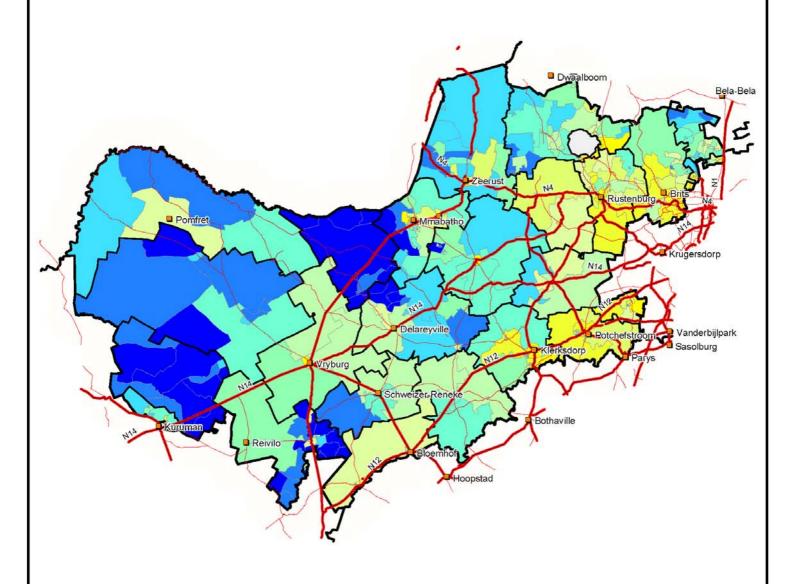
Map 5 - KwaZulu-Natal Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles



Map 6 - North West Province Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles

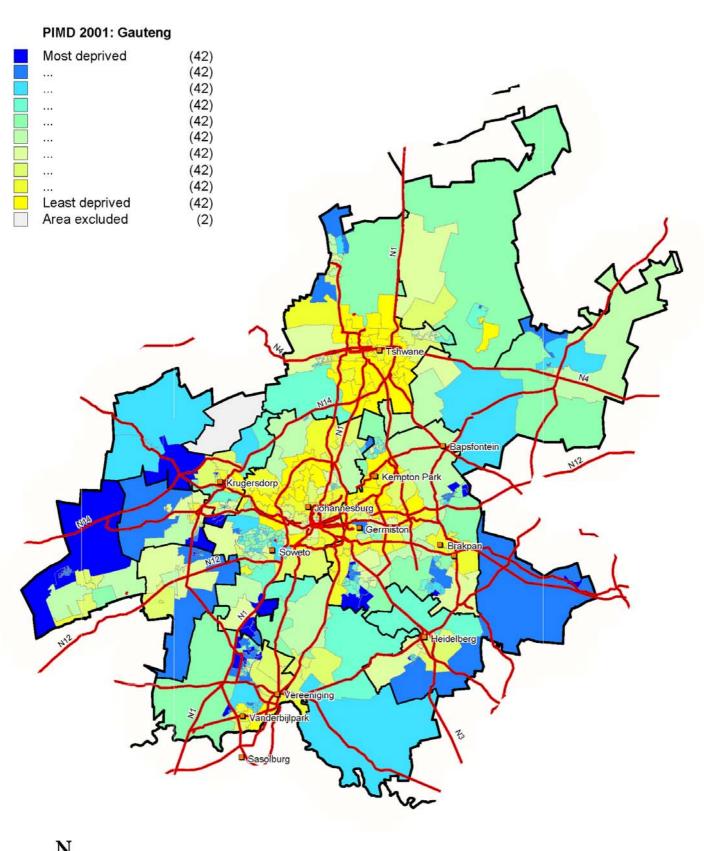
#### PIMD 2001: North West Province

Most deprived	(37)
***	(38)
***	(37)
	(38)
67	(38)
	(37)
***	(35)
•••	(37)
•••	(38)
Least deprived	(37)
Area excluded	(5)





# Map 7 - Gauteng Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles

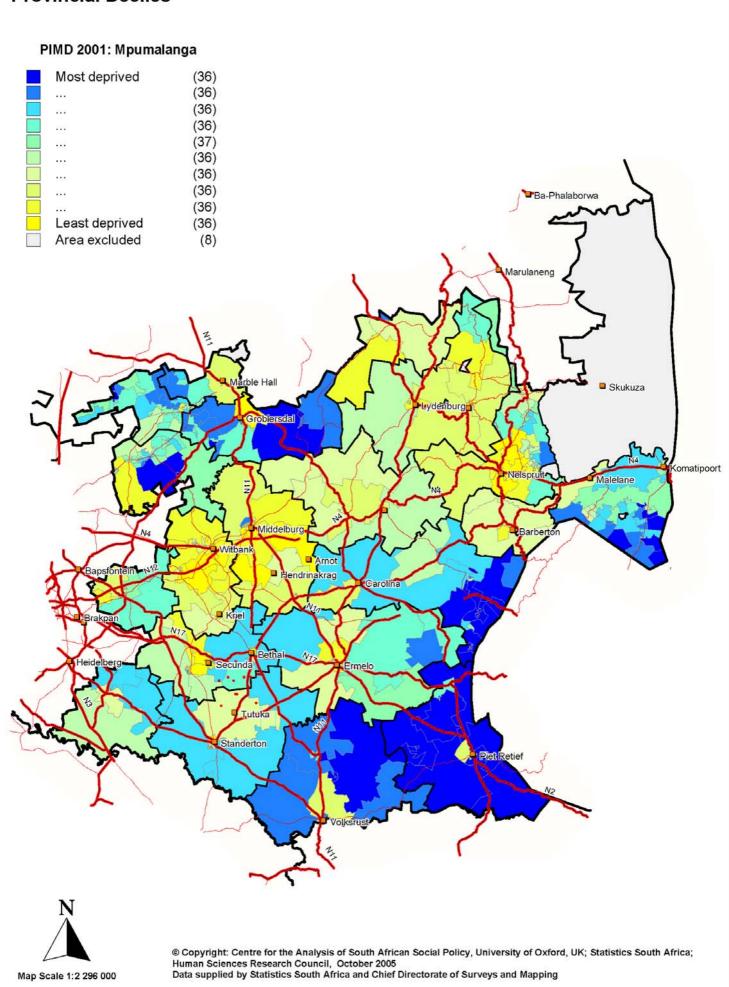




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Data supplied by Statistics South Africa and Chief Directorate of Surveys and Mapping

Map Scale 1:1 101 000

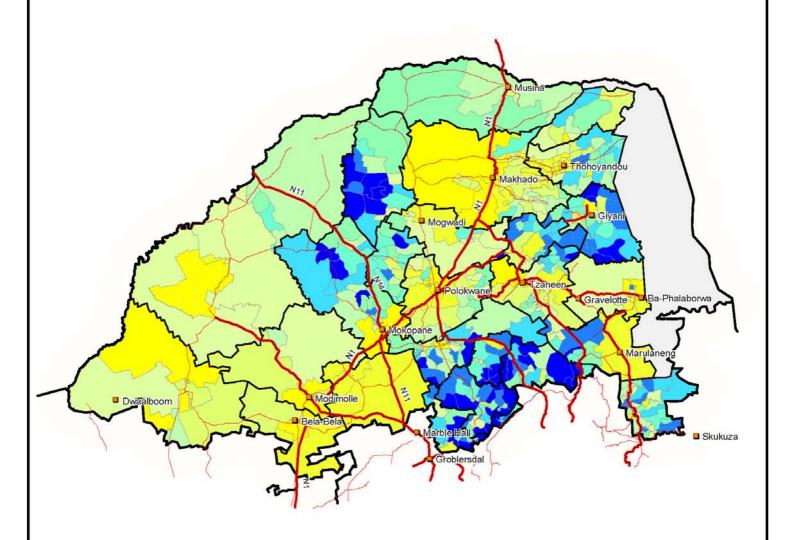
Map 8 - Mpumalanga Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles



Map 9 - Limpopo Index of Multiple Deprivation 2001 at Ward Level Provincial Deciles

#### PIMD 2001: Limpopo

	Most deprived	(45)
	***	(48
	***	(47
	***	(49
	222	(49
	***	(48
	***	(49
1.	***	(49
	m	(49
	Least deprived	(48
	Area excluded	(4





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